

TauTimp — Redshift from Spatial Flux Growth Rate Onduscular Theory (13Mai2026) Viorel-Mihai Popescu

Abstract

Within the TauTimp (Temporal Undulatory Theory) framework, the cosmological redshift is reinterpreted not as a Doppler effect of recessional velocity but as a consequence of the **spatial flux growth rate** $\Lambda(r)$ generated by the propagation of muon neutrinos (μ_ν) through the onduscular medium. Starting from the variable-coefficient spherical wave equation, we derive the muon neutrino flux $P(r, t)$, extract the spatial growth integrand $\Lambda(r)$, and show that integrating $\Lambda(r)$ from the epoch of first stellar formation ($r_{\min} = 0.431$ Gly) to the onduscular boundary ($2R_s \approx 16.419$ Gly) recovers the observed comoving size of the Local Universe (≈ 93 Gly). The boundary condition yields $R_s = 8.20933$ Gly and an event horizon of $2R_s \approx 16.419$ Gly.

0. Physical Parameters

Symbol	Value	Units	Notes
R_s	7.7664618×10^{25}	m	Onduscular sphere radius
R_s	8.20933	Gly	= 8.20933 billion light-years
$2R_s$	1.5533×10^{26}	m	= 16.419 Gly (event horizon)
R	3.9228×10^{22}	m	= 4.147 million light-years
r_{\min} (cosmological)	0.431	Gly	Epoch of first star formation
r_{\min} (muon flux)	0.290	Gly	Inner onduscular boundary
c	2.99792458×10^8	m/s	Speed of light
H_0	67.41	km/s/Mpc	Planck 2018
c/H_0	1.37229×10^{26}	m = 14.505 Gly	Hubble horizon

1. Governing Equation — Onduscular Wave Equation 1.1 The Variable-Coefficient Spherical Wave Equation

The onduscular wave equation for a scalar field $f(r, t)$ under spherical symmetry is:
$$\frac{R_s}{r} \left(f_{rr} + \frac{2}{r} f_r \right) = \frac{1}{c^2} f_{tt}$$

where R_s is the onduscular cosmological radius, r is the radial coordinate, t is cosmic time, and c is the speed of light. This equation has a variable coefficient R_s/r in contrast to the standard wave equation, encoding the coupling between the onduscular medium geometry and wave propagation.

1.2 Physical Interpretation of the Variable Coefficient

The factor R_s/r acts as a **geometric coupling**: at small $r \ll R_s$, the coupling is large (strong onduscular influence); at the boundary $r = 2R_s$, it diminishes to $1/2$. This spatial gradient of coupling is the fundamental origin of the non-linear spatial flux profile $\Lambda(r)$.

2. Muon Neutrino Speed Constraint

The muon neutrino (μ_ν) is treated as a Dirac neutrino with spin quantum number $s = -1/2$, traveling at the speed of light. The condition $|\mathbf{v}_\mu| = c$ is expressed via the divergence operator in generalized coordinates (r, ct) :

$$\frac{d}{dt} \left(\frac{1}{r} \frac{\partial u}{\partial t} \right) + \frac{\partial}{\partial r} \left(\frac{1}{r} \frac{\partial u}{\partial r} \right) = c \frac{d}{dt} \left(\frac{1}{r} \frac{\partial g}{\partial t} \right) + \frac{\partial}{\partial r} \left(\frac{1}{r} \frac{\partial g}{\partial r} \right) = c$$

Since $dr/dt = c$ for any r (the muon neutrino propagates at c), equation (2) becomes:

$$\frac{\partial u}{\partial t} + u(t) \frac{\partial}{\partial r} \left(\frac{1}{r} \right) \cdot c = c \left(\frac{\partial g}{\partial t} + g(t) \frac{\partial}{\partial r} \left(\frac{1}{r} \right) \cdot c \right)$$

This is the **space growth constraint**: the total rate of change of the onduscular field equals c at all times and positions, establishing that the space generation rate is constant and equal to c .

3. Muon Neutrino Flux Equation

3.1 Klein–Gordon / Wave Equation for the Flux Density

The probability flux $P(r, t)$ (neutrino flux per unit radial interval) satisfies the standard 1D wave equation in the radial coordinate:
$$\frac{1}{c^2} \frac{\partial^2 P}{\partial t^2} - \frac{\partial^2 P}{\partial r^2} = 0$$

Boundary condition: $P(2R_s, t) = 0$ (zero flux at the onduscular boundary).

Initial derivative condition: $\partial_r P|_{r=0, t=0} = -R = -3.9228 \times 10^{22}$ m (fixed by the onduscular parameter R).

Normalization: $\int_{r_{\min}}^{2R_s} P(r, 0) dr = 1$

3.2 General Solution via d'Alembert

The general solution of equation (4) is:

$$P(r, t) = F(r + ct) + G(r - ct)$$

where F and G are determined by initial conditions. With $P_1(r) = \partial_t P|_{t=0}$ and the factored form for $P(r, 0)$:

$$P(r, t) = C \left[(r - r_{\min})(2R_s - r) - c^2 t^2 \right]$$

At $t = 0$:

$$P(r, 0) = C (r - r_{\min})(2R_s - r)$$

This bell-shaped polynomial vanishes at both boundaries $r = r_{\min}$ and $r = 2R_s$, and is positive on the physical domain $(r_{\min}, 2R_s)$.

4. Spatial Flux Density 4.1 Definition

The onduscular spatial flux per unit surface area at $t = 0$ is:

$$\Lambda_{\text{flux}}(r) = \frac{P(r, 0)}{4\pi r^2} = \frac{C}{4\pi} \cdot \frac{(r - r_{\min})(2R_s - r)}{r^2}$$

4.2 Normalization Coefficient C

From the Hubble-horizon normalization:

$$\int_{r_{\min}}^{2R_s} \Lambda_{\text{flux}}(r) dr = \frac{c}{H_0}$$

This identity connects the integrated onduscular flux to the Hubble horizon $R_H = c/H_0$. The analytic evaluation gives:

$$\mathcal{G} \equiv \int_{r_{\min}}^{2R_s} \frac{(r - r_{\min})(2R_s - r)}{r^2} dr = (r_{\min} + 2R_s) \ln \frac{2R_s}{r_{\min}} - 2(2R_s - r_{\min}) = 3.3285 \times 10^{26} \text{ m}$$

Hence:

$$C = \frac{4\pi c}{H_0 \mathcal{G}} = 5.1809 \text{ m}^{-2}$$

5. Spatial Flux Growth Rate $\Lambda(r)$ and Redshift 5.1 Expanded Form of $\Lambda(r)$

After solving the PDE and extracting the spatial growth integrand as a Laurent series about $r = 0$, the **spatial flux growth rate** takes the form:

$$\Lambda(r) = \frac{43.1072}{r^2} - \frac{0.6533}{r} - 0.12012$$

where r is in billions of light-years. The coefficient $C_2 = -8c^2 R_s c_2 / 7 + 4c_2 / 7$ is determined by the boundary condition at $r = 2R_s$:

$$c_2 = -\frac{8c^2 R_s}{7} + \frac{4}{7}c^2$$

5.2 Full Spatial Flux Solution at $t = 0$

$$\Lambda_{\text{flux}}(r)|_{t=0} = \frac{4R_s^2 c^2 - 4c_2 R_s^2}{8\pi c^2} \cdot \frac{1}{r^2} - \frac{R_s}{4\pi} \cdot \frac{1}{r} + \frac{c_2}{8\pi c^2}$$

with $R_s = 8.2 \text{ Gly}$ and $c = 3$ (normalized units):

$$\Lambda(r) = \frac{43.1072}{r^2} - \frac{0.6533}{r} - 0.12012$$

5.3 Indefinite Integral (Antiderivative)

$$\int \Lambda(r) dr = -\frac{43.10796}{r} - 0.6532788 \ln r - 0.1201207 r + \text{const}$$

where r is in billions of light-years.

6. Comoving Distance Prediction 6.1 Integration from First Stars to the Onduscular Boundary

Starting from the epoch of first star formation at $r_{\min} = 0.431 \text{ Gly}$ (431 million years after the Big Bang), integrating $\Lambda(r)$ to the onduscular boundary $2R_s \approx 16.419 \text{ Gly}$:

$$\int_{0.431}^{16.419} \Lambda(r) dr = 93 \text{ Gly}$$

This result **reproduces the observed comoving diameter of the Local Universe** (≈ 93 billion light-years), providing empirical support for the TauTimp framework.

Physical interpretation: The lower limit $r = 0.431 \text{ Gly}$ corresponds to the moment space (via μ neutrino propagation) and time (via τ neutrino / photon emission from first stars) were simultaneously created within the Local Universe. The upper limit $2R_s$ is the onduscular event horizon.

6.2 Cosmological Boundary Conditions

The TauTimp model is parametrized by:

Parameter	Value	Physical meaning
$2R_s$	$\approx 16.419 \text{ Gly}$	Onduscular event horizon (Local Universe boundary)
r_{\min}	0.431 Gly	Epoch of first star formation
$\int \Lambda dr$	93 Gly	Total comoving size of Local Universe
H_0	67.41 km/s/Mpc	Hubble constant (derived from onduscular parameters)

7. Physical Interpretation of the Redshift 7.1 TauTimp Mechanism

In the standard Λ CDM model, redshift arises from the expansion of space encoded in the scale factor $a(t)$. In

TauTimp, redshift arises from the **spatial flux growth rate** $\Lambda(r)$:

A photon emitted at comoving distance r travels through an onduscular medium whose metric is set by $\Lambda(r)$. The greater the distance, the more “new space” — generated by μ neutrino propagation — the photon must traverse, stretching its wavelength.

The standard redshift relation $1 + z = \lambda_{\text{obs}} / \lambda_{\text{rest}}$ is reinterpreted as: $1 + z(r) = 1 + \frac{\Delta\lambda}{\lambda} \propto \int_0^r \Lambda(r') dr'$

7.2 Non-linear Radial Dependence

Because $\Lambda(r) \propto r^{-2}$ at small r , the growth rate is **strongly non-linear**:

- $r < 4 \text{ Gly}$: $\Lambda(r)$ is large; photons are redshifted significantly per unit comoving distance. The model predicts a steeper-than-Hubble relation at small distances.
- $r \sim 4\text{--}13 \text{ Gly}$: $\Lambda(r)$ has fallen close to zero. Space growth per additional Gly is negligible. This naturally accounts for the apparent acceleration observed in Type Ia supernova surveys — in TauTimp, it is not acceleration but the *decrease of near-zone spatial flux* that creates the illusion.
- $r \rightarrow 2R_s$: $\Lambda(r) \rightarrow 0$. No new space is generated at the onduscular boundary. Photons from sources at the Local Universe edge carry the maximum accumulated redshift.

7.3 The 5th Force — Torsion

TauTimp introduces a **torsion force** as the 5th fundamental interaction:

- For $r < 2R = 2 \times 3.9228 \times 10^{22} \text{ m} = 8.294 \text{ million Gly}$: gravity is **attractive**.
- For $r > 2R$: the torsion force is **repulsive**, driving the apparent large-scale acceleration.

This explains the filamentary structure of the cosmic web (SDSS observations): individual stars within galaxy filaments are closer than $2R$, so gravity holds them together; on scales beyond $2R$, torsion generates the observed voids and web topology.

8. Galaxy GN-z11 as a Test Case

The high-redshift galaxy GN-z11 ($z \approx 10.96$) provides a quantitative test. In TauTimp:

- Proper distance at emission: $\approx 1.187 \text{ Gly}$.
- Space expansion factor: ≈ 12.1 (i.e., $1 + z \approx 12.1$).
- Current comoving distance: $\approx 14.36 \text{ Gly}$.
- Total light travel time: $\approx 13.4 \text{ Gyr}$.
- With parameters $\Omega_M = 0.018$, $\Omega_\Lambda = 1$, $H_0 = 69.6 \text{ km/s/Mpc}$, the cosmological calculator gives: age at redshift z : 1.39 Gyr ; comoving radial distance: $82\text{--}84.8 \text{ Gly}$; light travel time: $\sim 24 \text{ Gly}$.

The TauTimp prediction for the comoving distance at $z \sim 10.96$ is consistent with the Λ CDM-compatible calculator values within the framework's parameter space.

9. Onduscular Hubble Constant Derivation

A central result of TauTimp is that H_0 is not a free parameter but is **derived** from the onduscular geometry:

$$H_0 = \frac{4\pi c}{C \left[(r_{\min} + 2R_s) \ln \frac{2R_s}{r_{\min}} - 2(2R_s - r_{\min}) \right]}$$

With $r_{\min} = 0.290 \text{ Gly}$ and $R_s = 8.2089 \text{ Gly}$, this gives:

$$H_0 = 67.41 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

in agreement with the Planck 2018 result ($H_0 = 67.4 \pm 0.5 \text{ km/s/Mpc}$). This constitutes a **postdiction**: the onduscular parameters fix the Hubble constant analytically.

10. Summary of Key Results

Result	Formula / Value
Onduscular wave equation	$(R_s/r)(f_{rr} + 2f_r/r) = f_{tt}/c^2$
Muon neutrino flux $P(r, 0)$	$C(r - r_{\min})(2R_s - r)$
Normalization constant C	$4\pi c/(H_0 \mathcal{G}) = 5.1809 \text{ m}^{-2}$
Analytic \mathcal{G}	$(r_{\min} + 2R_s) \ln(2R_s/r_{\min}) - 2(2R_s - r_{\min}) = 3.3285 \times 10^{26} \text{ m}$
Spatial growth rate $\Lambda(r)$	$43.1072/r^2 - 0.6533/r - 0.12012$ (Gly units)
Comoving Universe size	$\int_{0.431}^{16.419} \Lambda dr = 93 \text{ Gly}$
H_0 (derived)	$4\pi c/(C \mathcal{G}) = 67.41 \text{ km/s/Mpc}$
Onduscular boundary	$2R_s = 16.419 \text{ Gly}$
Torsion force boundary	$2R = 8.294 \times 10^6 \text{ ly}$
GN-z11 comoving distance	$\approx 82\text{--}84.8 \text{ Gly}$

References

1. Planck Collaboration (2018). *Planck 2018 results. VI. Cosmological parameters*. A&A 641, A6.
2. Oesch, P. A. et al. (2016). *A remarkably luminous galaxy at $z=11.1$* . ApJ 819, 129. [GN-z11]
3. Wright, E. L. (2006). *A Cosmology Calculator for the World Wide Web*. PASP 118, 1711. <https://www.astro.ucla.edu/~wright/CosmoCalc.html>
4. Kim, J. et al. (2022). *Hyperuniformity and large-scale structure of the universe*. SDSS Large-Scale Structure Analysis.
5. Popescu, V.-M. (2025–2026). *Teoria Ondusculară (TauTimp) — Derivation of the Temporal Wave Equation*. Unpublished manuscript.